

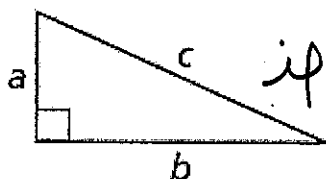
The Pythagorean Theorem

Lesson Objective INBAT use the Pythn. Thm and its converse, and classify Δ s.

One of the most famous theorems in mathematics is the Pythagorean Theorem, named for the ancient Greek mathematician Pythagoras. This theorem describes the relationship between the side lengths of a right triangle.

The Pythagorean Theorem

In a right triangle, the square of the length of the hypotenuse is equal to the sum of the squares of the lengths of the legs.



if rt. $\Delta \rightarrow a^2 + b^2 = c^2$

Pythagorean Triple: A Pythagorean Triple is a set of three positive integer (a, b, and c) that satisfy the equation $a^2 + b^2 = c^2$.

$\rightarrow$ no decimals

Common Pythagorean Triples

3, 4, 5	5, 12, 13	8, 15, 17	7, 24, 25
st = 2: 6, 8, 10	10, 24, 26	16, 30, 34	14, 48, 50
:	:	:	:
st = x: 3x, 4x, 5x	5x, 12x, 13x	8x, 15x, 17x	7x, 24x, 25x

Example:

1. Find the value of x. Then tell whether the side lengths form a Pythagorean Triple.

$$a^2 + b^2 = c^2$$

$$7^2 + x^2 = 14^2$$

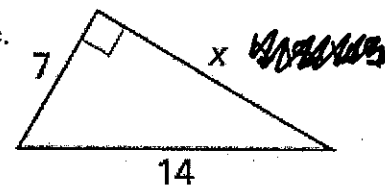
$$49 + x^2 = 196$$

$$\sqrt{x^2} = \sqrt{147}$$

$$x = \pm \sqrt{147}$$

$$x = \sqrt{49 \cdot 3}$$

$$x = 7\sqrt{3} \approx 12.12$$

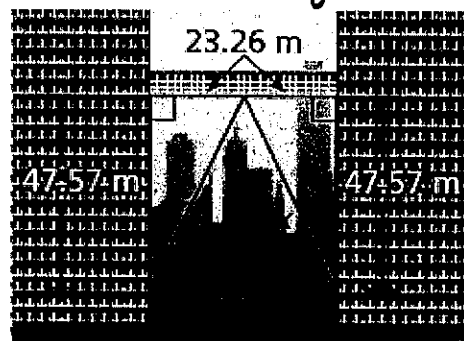


Not a triple b/c $7\sqrt{3}$ is not an integer!

2. The skyscrapers shown are connected by a skywalk with support beams. Use the Pythagorean Theorem to approximate the length of each support beam.

$$(47.57)^2 + (23.26)^2 = x^2$$

$$x \approx 52.95 \text{ m}$$



Using the CONVERSE of the Pythagorean Theorem

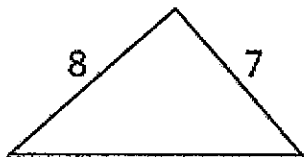
Conditional: If right triangle $\rightarrow a^2 + b^2 = c^2$

Converse: If $a^2 + b^2 = c^2 \rightarrow$ rt. Δ

Example:

3. Tell whether each triangle is a right triangle.

a.



$$8^2 + 7^2 \stackrel{?}{=} (\sqrt{113})^2$$

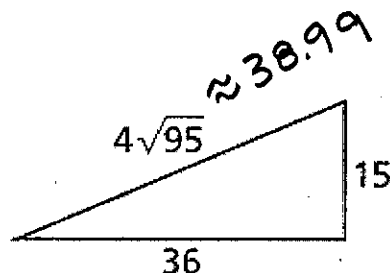
$$64 + 49 = 113$$

$$113 = 113 \checkmark$$

yes rt. Δ
b/c

$$a^2 + b^2 = c^2$$

b.



$$36^2 + 15^2 \stackrel{?}{=} (4\sqrt{95})^2$$

$$= (4)^2 (\sqrt{95})^2$$

$$= 16(95)$$

$$1521 \neq 1520$$

not a rt. Δ

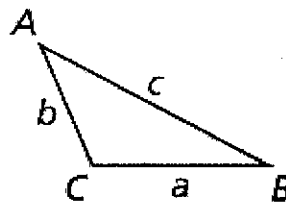
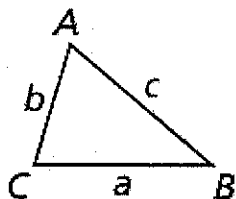
Classifying Triangles

Pythagorean Inequalities Theorem

For any ΔABC , where c is the length of the longest side, the following statements are true:

If $a^2 + b^2 > c^2$, then ΔABC is acute.

If $a^2 + b^2 < c^2$, then ΔABC is obtuse.



Example:

4. What type of triangle (if at all) do the following side lengths make? 4.3 feet, 5.2 feet, 6.1 feet c

$$4.3 + 5.2 > 6.1 \checkmark$$

$$5.2 + 6.1 > 4.3 \checkmark$$

$$4.3 + 6.1 > 5.2 \checkmark \text{ yes, } \Delta!$$

$$(4.3)^2 + (5.2)^2 \boxed{?} (6.1)^2$$

$$18.49 + 27.04 \boxed{?} 37.21$$

$$45.53 > 37.21$$

so the Δ is acute!

5. What type of triangle (if at all) do the following side lengths make? 3m, 4m, 6m c

$$3 + 4 > 6 \checkmark$$

$$3 + 6 > 4 \checkmark \text{ yes, } \Delta!$$

$$6 + 4 > 3 \checkmark$$

$$(3)^2 + (4)^2 \boxed{?} (6)^2$$

$$9 + 16 \boxed{?} 36$$

$$25 < 36$$

obtuse $\Delta!$